

## Rusho-Ramanujan Fourier Series

**Maher Ali Rusho** 

**Dedicated To**

My Father: Dr. Mohamamd Ali  
 My Mother and teacher of all time : Dr. Ruma Ali  
 My 2<sup>nd</sup> father : Engr. Ali Ahmmad Jewel  
 My 2<sup>nd</sup> Mother : and teacher of my early age Surraya Ahmed

**Abstract:** In the present realm of Mathematics the most beautiful and Exciting thing is infinitive, convergence series. When Ramanujan was young he plays with series and make new series . In this paper I have introduced an new point of view of convergency of pie . We will first prove 2 basic theoremas using fourier analysis then we sum up this and find the value of pie . And after that we will put it in the Ramanujan series and make a totally different series . Finally . this paper will be finished by a open question . Those who will find the answer, they please email me at : rusho.ali17@gmail.com. I will dedicate him in the next paper.

Here integration will be used by this symbol  $\int$   
 To express power the symbol '^' will be used  
 The symbol pie is expressed as  $\pi$   
 A notation is expressed as  $\sigma$

**Introduction**

Q(1) Find the fourier series expansion of  $f(x)=X$  in the interval  $(-\pi, \pi)$   
 Prove using fourier series

Let  $f(-x)=-x$  be a odd function . We know that for odd function fourier series is  
 $F(x)= \sum_{n=1}^{\infty} b_n \sin nx \dots \dots \dots (1)$

Here  
 $b_n = \frac{2}{\pi} \int_{0}^{\pi} f(x) \sin nx$   
 $dx = \frac{2}{\pi} \int_{-\pi}^{\pi} \cos n \frac{\pi}{\pi} = \frac{2}{n} (-1)^{n+1}$   
 $(2) = \frac{2}{\pi} \int_{-\pi}^{\pi} \cos n \frac{\pi}{\pi} = \frac{2}{n} (-1)^{n+1}$  By summing up we get  $\Rightarrow$   
 $F(x) = x = 2 \left[ \sin x - \frac{\sin 2x}{2} + \frac{\sin 3x}{3} - \frac{\sin 4x}{4} + \dots \dots \dots \right]$

Here  $x = \frac{\pi}{2}$  is the function evaluated. we find  
 $F(x) = \frac{\pi}{2} = 2 \left[ 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \dots \dots \dots \right]$

Then the series we find is

$$1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \dots \dots \dots = \frac{\pi}{4}$$

Again the function  $f(x) = \frac{\pi}{4}$  is evaluated we find :=

$$\frac{\pi}{4} = 2 \left[ \frac{1}{\sqrt{2}} - \frac{1}{2} + \frac{1}{3\sqrt{2}} - \frac{1}{6} + \dots \dots \dots \right]$$

$$\frac{\pi}{8} = \frac{1}{\sqrt{2}} \left( 1 + \frac{1}{3} - \frac{1}{5} - \frac{1}{7} + \frac{1}{9} + \frac{1}{11} + \dots \dots \dots \right)$$

$$= \frac{\pi}{4}$$

The series we found is

$$1 + \frac{1}{3} - \frac{1}{5} - \frac{1}{7} + \frac{1}{9} + \frac{1}{11} - \dots \dots \dots = \frac{\pi}{\sqrt{2}}$$

After summing up both equation we find :  $[\frac{\pi}{2} - \frac{2\sqrt{2}\pi}{8\sqrt{2}}] = 1$  or  $\pi = 16\sqrt{2} - 4\sqrt{2}$

From Ramanujan's series we find:  
 $2\sqrt{2} \sum_{k=0}^{\infty} \frac{(4k)! (1103 + 26390k)}{(k!)^4 (396)^{4k}}$   
 $= (2\sqrt{2} - 4) / 16\sqrt{2}$

Here it is the broken English Rusho Rmanujan series

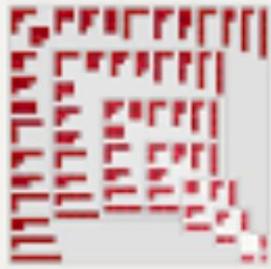
**The open problem and abstract**

*We all know the following Ramanujan - Hardy Partition formula*



### Hardy-Ramanujan Formula

Let  $p(n)$  be the number of partitions of  $n \in \mathbb{Z}$ . Then, as  $n \rightarrow \infty$  :

$$p(n) \sim \frac{1}{4\sqrt{3n}} e^{\sqrt{\frac{2n}{3}}\pi}$$


Src: <https://www.newscientist.com/article/dn20039-deep-meaning-in-ramanujans-simple-pattern/>

Can anyone tell me What if We put the negative value of n. Will the formula work for negative values. Will this formula work like minus 121 is a number. How many ways it can be partitioned. If The reader knows the answer then please contact with my website: [rusho.org](http://rusho.org) or email: [rusho.ali17@gmail.com](mailto:rusho.ali17@gmail.com)