

## Modelling Space-time Propagation of Climate Sensitive Variation in the Indus River Flow

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**Abstract:** The linear and nonlinear analyses of the impacts of local climatic parameters on Indus River flows as discussed in [1] and [2] gives provision to investigate the influential role of the regional climatic parameters. For this purpose this paper simulates the Indus River flow network using exponentially distributed river network (SRN) feed by employs synthetically generated local temperature and rainfall dependent runoff. The local temperature and rainfall is generated using the stochastic, autoregressive and Poisson process methods respectively. To explore the influential role, the sensitivity analyses are performed by changing the local climatic parameter values. This demonstrates the existence of relation between the variability of temperature and rainfall on the river flow in the form of linear and nonlinear information and its propagation along the network. In the mean 10daily flow (TDF) propagation the dominant precipitation characteristic is linear. It is to be saying that the temperature variations make some way of only nonlinear behaviour in the TDF propagation. Accordingly, it explores the impact of local climatic parameters on the river flow and its propagation in the form of linear and nonlinear information.

**Keywords:** Indus River, Local Climate, Propagation, River network

### 1 Introduction

Pakistan suffered a cluster of torrential rain events, causing the worst flooding in 100 years [3]. About 1700 people perished and 1.8 million homes were lost, rendering 20 million people homeless, with an economic loss estimated to be more than \$40 billion U.S. [4]. The arena of problems like correct assessment, proper storage, reliable control and judicious distribution of existing water masses among various provinces/regions within Pakistan is properly encompassed by technical research and mathematical modelling. Keeping in view the preliminary local climatic analyses as presented in Hassan and Ansari (2015) and linear and nonlinear analyses performed in Hassan and Ansari, (2010), and Hassan (2011) [1-5], this paper assess the impact of climatic parameters (Temperature & Rainfall) on mean 10daily river flow (TDF) along the Indus River.

A detailed knowledge of river geomorphology, river dynamics, their branching process and flood routing is fundamental for the analyses required for long-term flood forecasting and management. Study of river networks is, thus, very essential for this purpose. The setback with conventional statistical/probabilistic or stochastic networks is that they ignore the nonlinearity inherent in the problem. The river system network consists of links and nodes classically defined by work on tributaries and the interaction of main stream including junction hydraulics and mixing their work on the structure [6-9]. However, from mid-1980's, tributaries and the

network study grows rapidly on the interaction of morphology, hydraulics and sedimentology [10] and their basin hydrological response [11]. This field of research has matured to modelling the dynamics of their processes like geomorphology [12-14]. [11] relates the hydrologic response of the river basin to its geomorphology using fractal stream channel network. [15] utilizes runoff analysis engine of IFAS (Integrated Flood Analysis System) based on a 3-layered spatially distributed tank model for rainfall runoff analysis to simulate the flood events of 1992, 1994 and 2012 based on the calibration of 1988, 1997 and 2010 flood evaluation based on Nash-Sutcliffe efficiencies. [16] determine annual and intra-annual oscillations of the local rainfall seasonality and interannual to interdecadal changes linked to large scale circulation patterns like El Niño/Southern Oscillation, the North Atlantic Oscillation, and the Interdecadal Pacific Oscillation. The results based on the analysing of hydroclimatic time series using a data-driven method named Complete Ensemble Empirical Mode Decomposition with Adaptive Noise (CEEMDAN) applied to the Paraná River monthly discharge. [17] consider the Conformal-Cubic Atmospheric Model of CSIRO Australia and Regional Climate Model to investigate about recent and the predicted twenty first century climatic and hydrological changes over the mountainous Upper Indus Basin. However, they utilize predefined model to performed future projections and fails to provide the impact of local climatic parameter on different river flow variations. For this purpose, this study



construct an exponentially distributed river network (SRN) for the simulation of Indus River. This SRN utilizes synthetically generated local temperature and rainfall (details discussed in next sections) to replicate the Indus River flow. To check the existence and propagations of linear and nonlinear information (components) in this river flow, the sensitivity analyses will performed by changing the average climatic parameter values. These analyses will demonstrate any possibility of existence of a relation between the variability of local climatic parameters and the river flow in the form of linear and nonlinear information and its propagation along the network. Moreover, the outcomes tell us about the impact of local climatic parameters on the river flow and its propagation.

The sec. 2.1 will perform simulation of the Indus River flow and comparison between the behaviours of real and simulated river flow propagation Patterns along the Network. Sec. 3 deals with results and discussion related to Influence of Climatic factors on River Flow Propagation and finally sec. 4 conclude the paper

## 2. Materials and Methods

### 2.1 Simulated Modelling of the River Network

For simulation of River network, construct a SRN, and customise it to match the Indus River network

(Table 1). It is assumed that the catchment areas and the inter-catchment distances of the network are exponentially distributed (Table 2). This networked has a main stream starting as an outsourcing of a big main catchment and other catchments are linked in the downstream. It is further assumed that the main catchment area is about 75% (to simulate Upper Indus Basin above Tarbela), and the sum of the other catchments are being 25% (catchments of the Indus River below Tarbela) of the total of all catchment areas (Fig. 1). The generated inter-catchment distances of SRN only considers catchment-1, 2, 3, 4, 6, 7 and 9 because they are in close relation to that of Indus River network (Table 1 & 2). The altitudinal range of each catchment is obtained from linearly approximated general hypsometric curve [18] of the UIB region (Fig. 2, Table 3). To feed these catchments, the daily sum of precipitation is synthetically generated by Poisson process and the daily mean temperature (MDT) is generated by using autoregressive AR(2) model [19]. The mean annual temperature decreases with increasing altitude values (Table 4). To simulate these variations, the approximately estimated temperature lapse rate value is about  $-0.0065\text{ }^{\circ}\text{C m}^{-1}$  (Table 4). To setup the elevation dependent annual sum of precipitation lapse rate, break the 4 to 7500m altitude range in to three ranges 4–500m, 500–1250m and 1250–7500m.

**Table 1** Reference station related distances from lower three stations all their upstream stations along Indus River. All distances are in canal km (Source: Irrigation and power department, Government of the Punjab, Lahore)

Distances from ↓ to ⇒	Sukkur	Guddu	Taunsa	Chasma	Kalabag	Tarbela
Kotri	479.57	690.39	991.33	1235.94	1334.11	1535.27
Sukkur	0.00	209.21	511.76	756.37	854.54	1055.70
Guddu		0.00	302.55	547.16	645.33	846.49

**Table 2** Detail of exponential distributed all inter-catchment distances and accumulated catchments distances from catchment-9 to catchment-1

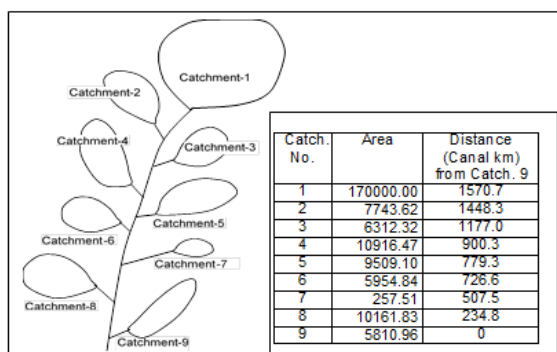
From Catchmen to Catchmen	Distance between two Catchments (Km)	Accumulated distance from Catchment-9 to Catchment-1 (Km)
1- to - 2	122.327	1570.669
2- to - 3	271.321	1448.343
3- to - 4	276.740	1177.021
4- to - 5	120.975	900.282
5- to - 6	52.741	779.306
6- to - 7	219.029	726.565
7- to - 8	272.754	507.536
8- to - 9	234.782	234.782

**Table 3** Detail of all catchments altitudinal ranges with its minimum and maximum altitudinal values

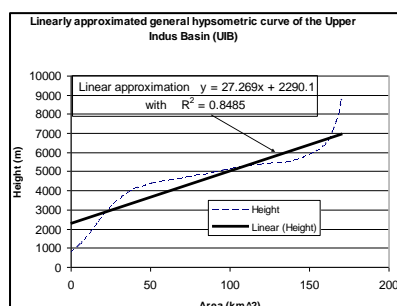
No.	Area (km <sup>2</sup> )	Altitude range (km)	Altitude range with in catchment (m)	
			Minimum	Maximum
1	170000.00	7.0	500	7500.00
2	7743.62	0.319	400	718.855
3	6312.32	0.260	350	609.919
4	10916.47	0.450	300	749.502
5	9509.10	0.392	275	666.551
6	5954.84	0.245	250	495.199
7	257.51	0.011	225	235.603
8	10161.83	0.418	150	568.428
9	5810.96	0.239	100	339.275

**Table 4** Temperature lapse rates based in Annual mean temperature during 1977-97 of available cites data out of these approximately  $-0.0065^{\circ}\text{C m}^{-1}$  lapse rate is selected

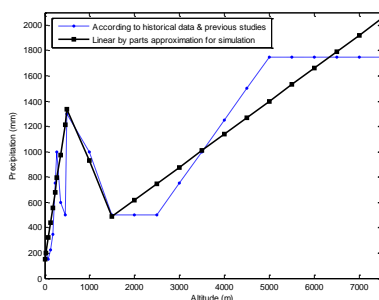
City	Altitude (m)	Annual Mean Temp. ( $^{\circ}\text{C}$ )	Name of the two cities lapse rates (LP)	Lapse rate (LP) between two cities ( $^{\circ}\text{C m}^{-1}$ )
Skardu	2181	11.83690	Skardu - Gilgit	-0.0054
Gilgit	1459	5	Gilgit - Kakul	-0.0039
Kakul	1309	7	Kakul - Karachi	-0.0079
Karachi	4	16.35	Average of above three LP	-0.0058
		26.66	Overall LP (Skardu – Karachi)	-0.0068
			Average of above two LP	-0.0063



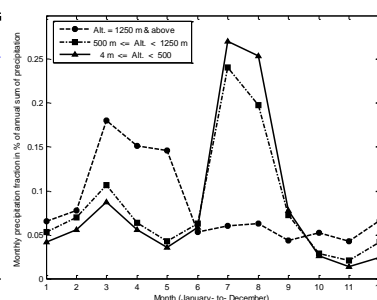
**Fig. 1** Structure of the exponentially distributed river network (EDRN) to simulate the Indus River.



**Fig. 2** linear approximation of the general hypsometric for the upper Indus basin (UIB) defined by Hewitt, (1993) (Hewitt, 1993) above Tarbela Dam showing approximate altitudes of precipitation zones. The curve is derived from 2000ft contour intervals on map sheet of the area at scale of 1:250,000. The linear equation is  $y = 27.269x + 2290.1$ , where  $x$  is the area in  $\text{km}^2$  and  $y$  its relative height in km, with residual sum of square  $R^2 = 0.8485$ . This linear approximation is used to set the altitudes with in each catchment of EDRN



**Fig. 3** Annual sum of precipitation (1977–97) with respect to altitude provide precipitation lapse rate according to the historical data and previous studies (---), we linearly approximate these lapse rate by parts (—) in to



**Fig. 4** Three pattern of SMP in fraction of % according to the annual sum of rainfall for the altitude range divided in to three regions.

**Table 5** Sum of monthly precipitation (in percentage) according to the annual sum of rainfall of the each altitude range

Month	4 m to 500 m	501 m to 1250 m	1251 m & above
Jan	0.042011	0.053058	0.065328
Feb	0.055755	0.069959	0.077936
Mar	0.086920	0.106382	0.179840
Apr	0.056105	0.063459	0.151075
May	0.035908	0.042716	0.145950
Jun	0.057966	0.063066	0.052851
Jul	0.271051	0.240994	0.060393
Aug	0.253787	0.197710	0.062752
Sep	0.077310	0.072530	0.043284
Oct	0.025490	0.028420	0.051911
Nov	0.013601	0.020397	0.042526
Dec	0.024097	0.041309	0.066154

## 2.2 Catchments' Runoff Generation

To feed the modelled SRN, synthetically generated precipitation and temperature dependant snow-glacier melt runoffs are utilized to produce the daily outflow of each nine catchments with following model (Fig. 5):

$$\frac{dW}{dt} = kR_R^\alpha + M_S + M_G - L_c - rW^\beta \quad (1.2)$$

where  $W$  is the catchment water production,  $kR_R^\alpha$ ,  $M_S$  and  $M_G$  are the rainfall, snow melt glacier melt runoffs respectively. Whereas  $L_c$  (section 2.2.2) and  $rW^\beta$  is the portion of storage to form outflow ( $\beta = 1$  for linear). The schematic diagram of Fig. 5 provides an understanding of the working of the module apply to all catchments with following assumptions.

- (i) If the daily temperature  $\leq 2^\circ\text{C}$  so, the falling precipitation will be snow otherwise it is rainfall. Moreover, new snowfall is added to snowpack, glacier region or plain ground, as water equivalent.
- (ii) Rainfall runoff (liquid accumulates) promptly contributes to river flows whereas, the snowmelt runoff provides a delayed base flow the catchment runoff.
- (iii) If the daily temperature increases from the threshold  $T_h = 0^\circ\text{C}$ , it is assumed that snowmelts is at the rate of  $1.5 \text{ mm } ^\circ\text{C}^{-1} \text{ day}^{-1}$ . when all the liquid and snowpack are depleted in the glacier region the ice melt occurs at the rate of  $4 \text{ mm } ^\circ\text{C}^{-1} \text{ day}^{-1}$  [21].

**Temperature generation,** The annual patterns of mean monthly temperature (MMT) variations of all cities are approximately the same. The generation of MDT follows autoregressive AR(2) model added (superimposed) on the linear interpolated MDT value from historical annual pattern of MMT, and normally distributed noise and defined as :

$$T_t = d_t + b_1 T_{t-1} + b_2 T_{t-2} + e_t \quad (1.3)$$

Where  $T_t$  is the generated MDT at time  $t$ ,  $d_t$  is the linear interpolated MDT,  $b_1$  and  $b_2$  are the coefficients of the AR(2) terms  $T_{t-1}$  and  $T_{t-2}$  respectively and  $e_t$  is the normally distributed random noise with mean 0 and variance 1. This method may be capable in replicating the actual MDT and with help of temperature lapse rate (as defined above) they generates the MDT of all the catchments.

**The daily outflow module of the catchments,** Precipitation is the major source to produce runoff in the daily outflow module of the catchments (Fig. 5). The precipitations of these catchments are generated by marked Poisson process [22]. The daily generated precipitation events are summed up and their respective depth to the daily sum of precipitation in mm/day. If MDT value, is  $T_t < 2^\circ\text{C}$  the daily precipitations  $P$  will become snowfall  $P_s$  and if  $T_t \geq 2^\circ\text{C}$  then it will considered as  $P_R$  the rainfall. The daily rainfall  $P_R$  spikes transform in to rainfall runoff  $R_R$  [22] using:

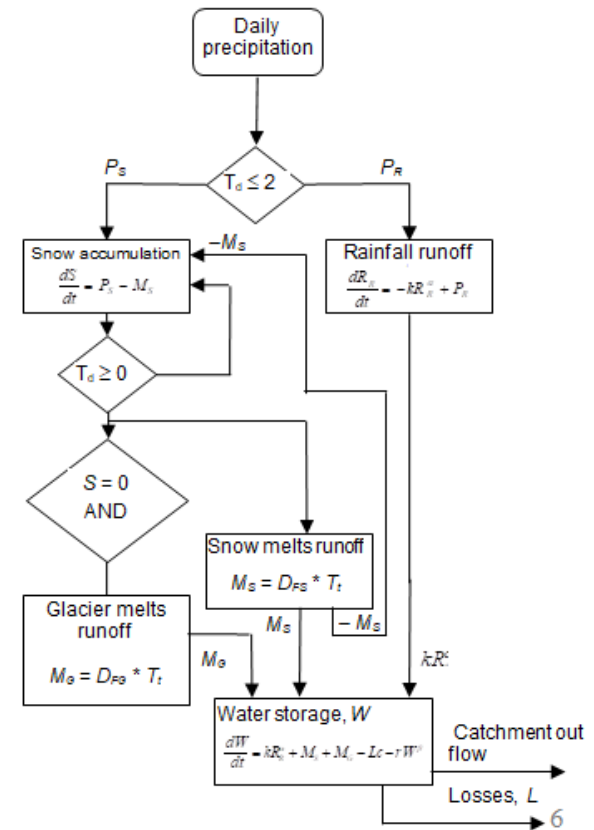
$$\frac{dR_R}{dt} = -kR_R^\alpha + P_R \quad (1.6)$$

where  $-kR_R^\alpha$  is the decay recession effect in  $R_R$ , and  $\alpha$  is the factor to set the decay recession flow and  $k$  represents the coefficient of recession flow. Moreover, the daily snowfall accumulates as liquid equivalents on the old accumulated snow, glacier, or ground as follows:

$$\frac{dS}{dt} = P_s - M_s \quad (1.7)$$

where  $dS/dt$  is the rate of variation in the snow accumulates,  $P_s$  and  $M_s$  are the daily snowfall, and

snowmelt runoff respectively (depends on degree-day factor  $D_{FS}$ ). When  $T_t \geq 0^\circ\text{C}$  then  $M_s = T_t D_{FS}$  and if snow cover vanish on the glaciated area then glacier melt starts with the degree-day factor of glacier  $D_{FG}$  as,  $M_G = T_t D_{FG}$ , where  $M_G$  is the daily glacier melt runoff value.



**Fig. 5** Schematic diagram of catchment daily outflow module based on rainfall runoff, snow and glacier melt runoffs components respectively

### 2.2.2 The generalized losses

This simulation method considers two types of water losses, evaporation and seepage, during runoff generation and the propagation of river flow along the SRN respectively.

**Evaporation in the catchment,** It is assumed that the minimum to maximum evaporation  $L_{ct}$  in the catchment are 0 to 5 mm/day respectively and are linearly dependant on the MDT ( $T_t$ ) of the catchment as:

$$L_{ct} = \left[ \frac{5}{(T_{tamx} - 2)} (T_t - 2) \right] \quad (1.8)$$

where  $L_{ct}$  is the straight line (linear) relation between  $(2^\circ\text{C}, 0 \text{ mm})$  and  $(T_{tamx}^\circ\text{C}, 5 \text{ mm})$  coordinates. Where  $T_{tamx}$  is the annual maximum MDT of the catchments. Moreover, to include the impact of daily rainfall on



the evaporation assume the following relation of  $L_{ct}$  to the net daily loss due to evaporation  $L_c$  (mm/day).

$$L_c = L_{ct} \left( 1 - \frac{P}{P_{amx}} \right) \quad (1.9)$$

where  $P_{amx}$  is the annual maximum daily precipitation, and  $P$  is the daily precipitation. Substituting the values of equation (1.6),  $M_s$ ,  $M_G$ , and (1.9) in the water storage equation (1.2) then get the outflow of the catchment  $Q = r W^\beta$ . The same procedure applies to all nine SRN catchments to generate the respective daily out flows.

To consider base flow from catchment-1 due to the ground water contribution of the deep snowpack and glacier areas [23-24] it is assumed that a fixed value of  $Q_b = 250 \text{ m}^3/\text{s}$  is generated from the catchment continuously. The out flow represented as  $Q_i^1 = Q_1 + Q_b$  and from the other catchments are  $Q_i^c = Q_c$ , where  $c$  is the catchment number and  $i$  is the day.

**Seepage along the River,** The seepage losses is assumed to be about 3% per 10 miles or  $0.186\% \text{ km}^{-1}$  [25]. The final flow  $F_f$  and the initial flow  $F_i$  are related as:

$$F_f = F_i (1 - 0.00186 d_t) \quad (1.10)$$

where  $d_t$  is the distance (km) travelled by water mass along the main stream.

Diffusion behaviour is introduced by multiplying the seven (7) days moving average river flow by lognormal weighted noise. To make real daily variations in the diffused (smooth) river flow add some lognormal distributed noise  $\varepsilon_i$  as

## 2.4 River flow propagation method

The daily outflow of each catchment needed some diffusive and velocity shifting behaviour to simulate the travelling of water mass along the main stream. Diffusion behaviour is introduced by multiplying the seven (7) days moving averaged river flow by lognormal weighted noise  $w_j$ . To make some real daily variations in the diffused (smooth) river flow add some lognormal noise  $\varepsilon_i$  as follows:

$$Q_i^N = \sum_{j=-3}^{+3} Q_{i+j}^N w_j + \varepsilon_i \quad ; \quad \text{where } Q_i^N \text{ is the}$$

diffused  $i^{\text{th}}$  river flow of the  $N^{\text{th}}$  catchment. The velocity shifting behaviour is introduced by some negative lag ( $e$  positions) shifting of the river flow values. The  $i^{\text{th}}$  river flow  $Q_i^N$  shifted to the lag  $= -e$  is defined as:  $Q_i^N = Q_{i-e}^N$ . Consider both diffusion and velocity shifting behaviour after each catchment

as  $Q_{i,d}^c$  (where  $i$  represents the  $i^{\text{th}}$  daily flow of the catchment- $c$  after the  $d^{\text{th}}$  catchment represent the location of the river flow record in SRN) as:

$Q_{i,1}^1 = Q_i^1 + Q_b$  where  $Q_{i,1}^1$  is the  $i^{\text{th}}$  daily flow of the catchment-1, and  $Q_b$  is the base. The remaining all flow records location after each catchment-2 to 9 in SRN is represented as:

$$Q_{i,d}^c = Q_i^c + \sum_{j=-3}^3 Q_{\{[i-e(c)]+j\}, c-1}^{c-1} * w_j + \varepsilon_i \quad ; \quad \text{where}$$

$Q_{i,d}^c$  is the  $i^{\text{th}}$  river flow record after location

$d$  and  $c$  is the catchment number ( $c = 2, 3, 4, 5, 6, 7, 8, 9$ ). After generating daily river flows of each location of the SRN, convert all of them to the 10daily river flows (TDF)  $Q_{Ti,d}^c$  for the further LM and NLM analysis.

## 3.1 Comparison between the behaviours of real and simulated river flow propagation Patterns

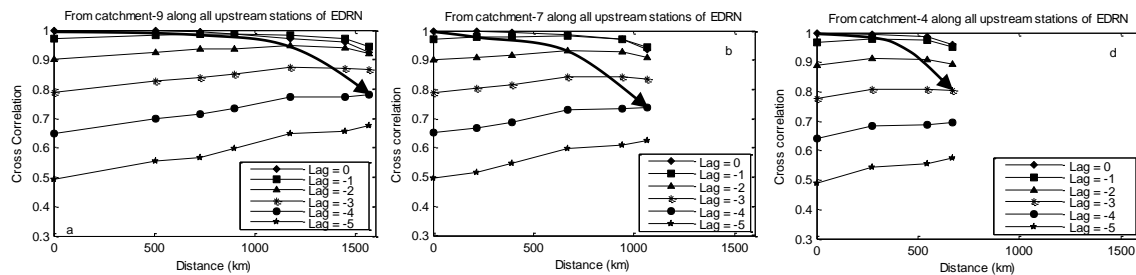
To calibrate TDF of the main stream generated by catchment-1 compare with the TDF of Tarbela station. This shows a better simulation of the 10daily out flow at Tarbela station. The next step will simulate the behaviour of cross correlation (CC) and normalized cross mutual information (MI) of the Indus River and the generated TDFs'.

The Fig. 6a shows the CC analysis between catchment-9 (last station of SRN) with itself and with all its upstream stations (catchment-7, 6, 4, 3, 2, & 1). It also represents proper simulation of the real LP curve as mention in Fig. 4.3a of Hassan (2011) however, a relatively slower roll off of simulated LP curve found. This behaviour happened because the simulation utilized limited number of dominating parameters instead of large number of actual parameters involved in the real river flow. Repeat the same procedure for catchment-7 and catchment-4 (Fig. 6b & c) and skip the catchment-6 because it does not match the contours of the real LP curves from third last station (Guddu). The above simulation showed by using CC analysis of TDF it is clear that the contours of the real LP curves as mention in Fig. 4.3a of Hassan & Ansari (2011) and the simulated LP curves (Figs. 6a-c) are similar.

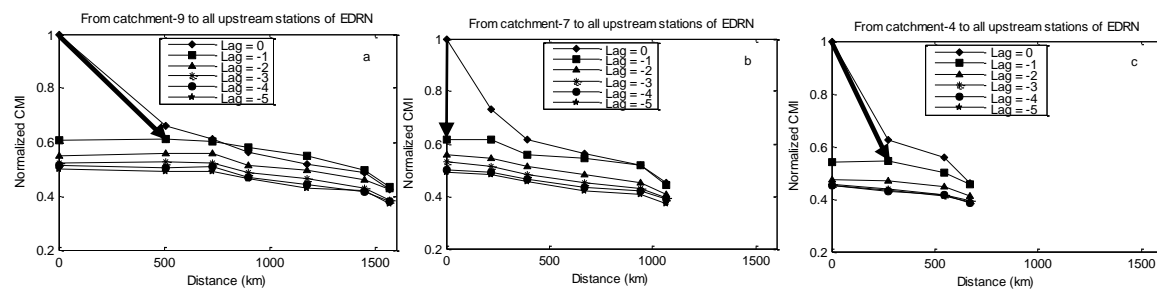
The simulation of NP curves of the Indus TDF using MI analysis [5] is performed by generated TDF of SRN. It is observed that the simulated NP curve based on MI analysis between catchment-9 with itself and with all its upstream stations catchment-7, 6, 4, 3, 2, & 1 (Fig. 7a) is similar to the real NP curve between Kotri with itself and all its upstream stations

Fig. 4.4a of [5]. The NP curves from the last three reference stations in real network and from catchment-9, 7, & 4 in the SRN simulated NP curves are similar (Fig. 7a-c). To explore the impact of real local climatic variability in the river flow, the next

section analyses the variations in the propagation of linear and nonlinear information (LP and NP curves) under the climatic influence along the whole SRN network.



**Fig. 6** Linear information propagation roll-off (LIPR) behaviour obtain from distance dependent CC analysis of the EDRN simulated Indus River (simulate the space-time cross-correlation analysis along the Indus River Fig. 4.3 of Hassan (2011)), from lower three stations separately with itself and with all their selected upstream stations of EDRN: (a) from catchment-9, (b) from catchment-7, and (c) from catchment-4



**Fig. 7** Nonlinear information propagation roll-off (NLPR) behaviour obtain from distance dependent CMI analysis of the EDRN simulated Indus River (simulate the space-time cross-correlation analysis along the Indus River Fig. 4.4 of Hassan (2011)), from lower three stations separately with itself and with all their selected upstream stations of EDRN: (a) from catchment-9, (b) from catchment-7, and (c) from catchment-4

### 3: Results and Discussion

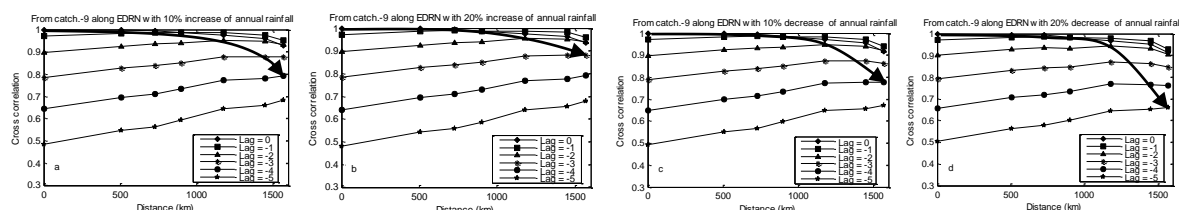
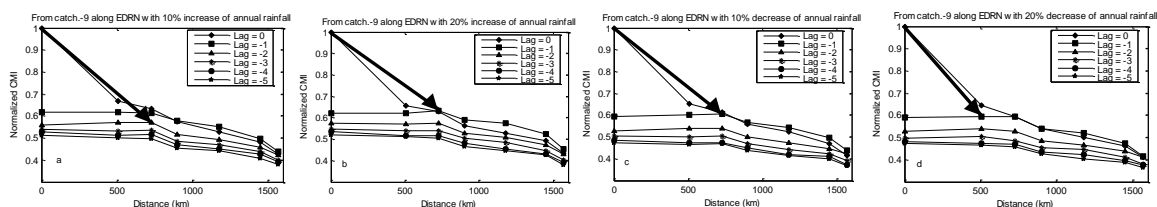
This section will show how temperature and rainfall variations influence the river flow and its propagation. To implement this idea analyse the changes in LP and NP curve (Fig.6 & 7) variations by introducing some changes in the normally simulated temperature and rainfall values.

**Impact of rainfall variations,** To observe linear influence in the river flow propagation introduce 10% and 20% increase in the simulated annual sum of rainfall (ASRF) values. The results shows some gradually raise (or slow roll-off) in the simulated CC value curves (Fig. 6a). The resultant LP curves (Figs. 8a & b) demonstrate increasing trends. This trend is retains for 30%, 40%, and 50% increase in ASRF.

Moreover, the 10% and 20% decrease in the ASRF values, CC and LP curves shows gradual quick roll-off for each change (Figs. 8c & 8d). This trend continues for 30%, 40%, and 50% decrease in ASRF values. These variations explore that the increasing rainfall may behave linearly in the river flow propagation along the network. To explore the nonlinear effect of rainfall the simulated NP curve (Fig. 7a) propagates only to the next station (catchment-7, lag = -1). However, 10% increase in ASRF makes NP curve (Fig. 9a) to prolong more and end at a longer distance (catchment-6) and at lower lag (lag = -2). Further development in MI and resultant NP curve variations are shown in Table-6.

**Table 6** Impact of percentage  $\uparrow$  Increasing or  $\downarrow$  Decreasing variations in the annual sum of rainfall on the LIPR and NLPR curves behaviour that starts from Catchment-9, Lag-0

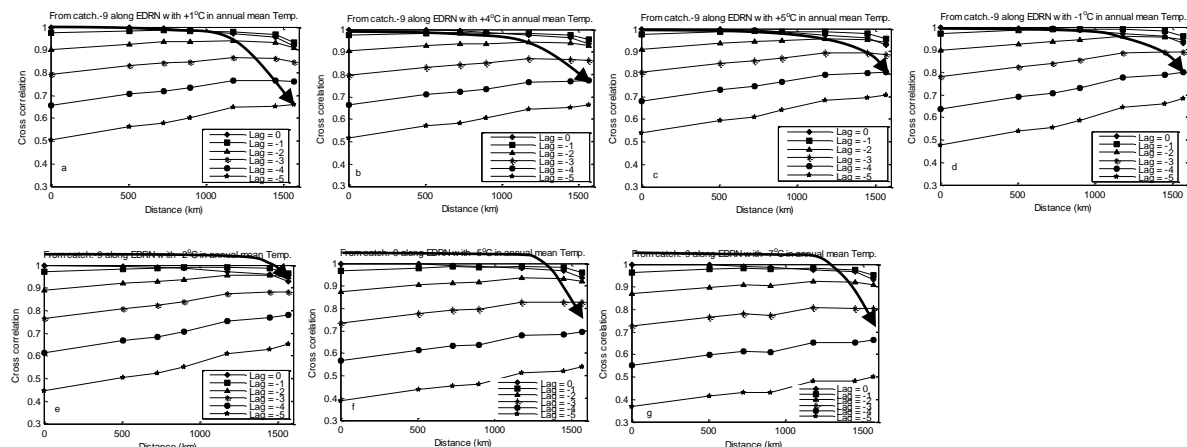
Fall of Propagation of LIPR curves		
Catchment No.	Lag No.	Percentage of $\uparrow$ Increasing, and $\downarrow$ Decreasing variations in the annual sum of rainfall
1	-3	20% $\uparrow$ , 40% $\uparrow$ , 50% $\uparrow$
1	-4	Normal, 10% $\uparrow$ , 30% $\uparrow$ , & 10% $\downarrow$
1	-5	20% $\downarrow$ , 30% $\downarrow$ , 40% $\downarrow$
2	-4	50% $\downarrow$
Fall of Propagation of NLPR curves		
7	-1	Normal, 20% $\downarrow$
7	-2	30% $\uparrow$
6	-1	20% $\uparrow$ , 40% $\uparrow$ & more; 10% $\downarrow$ , 30% $\downarrow$ & more
6	-2	10% $\uparrow$

**Fig. 8** Variations in the LIPR curve (based on CC value curves behaviour of the MTDRF along the EDRN from catchment-9 with itself and with all its selected upstream stations) at four different deviations in the normally simulated ASRF values: (a) 10% increase, (b) 20% increase, (c) 10% decrease, and (d) 20% decrease**Fig. 9** Variation in the NLPR curve (based on NCMI value curves behaviour of the MTDRF along the EDRN from catchment-9 with itself and with all its selected upstream stations) at four different deviations in the normally simulated ASRF values: (a) 10% increase, (b) 20% increase, (c) 10% decrease, and (d) 20% decrease

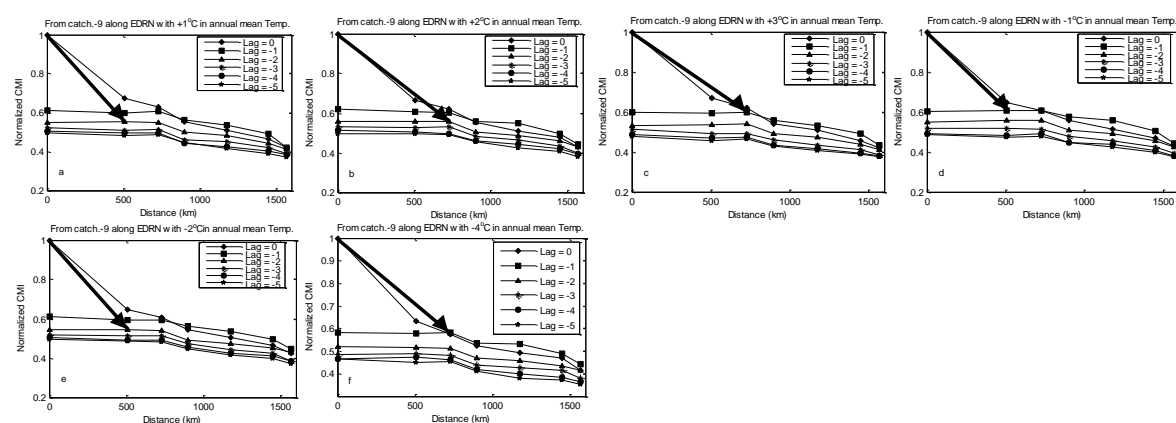
**Impact of temperature variations,** When AMT values increases from +1 to +3°C the CC value curves slightly loses their level and resultant LP curve shows slightly sharper roll-off, ending at same catchment-1 but at lower lag = -5 (Fig. 10a). Further +4 to +7 °C increase in the AMT value the CC curves gradually increase their levels and resultant LP curve increases to their normally simulated contours ending at same catchment-1 and lag = -4 (Figs. 10b & 10c). A reduce to -1°C in AMT value makes no significant change (Fig. 10d) in normally simulated CC and LP curve (Fig. 10a). A -2 °C reduce in AMT value increases the levels of normally simulated CC values and the resulting LP curve (Fig. 10e) ending at higher lag = -3. More reduction in the AMT value will gradually decrease these levels of CC values and the resulting LP curve sharply drops at the last three stations (Figs. 10f & 10g) ending at lowest lag = -5. For observing variation in the NP curves introduce

+1°C increase in AMT values makes no change in the normally simulated MI based NP curve (Fig. 11a) . Further +2°C increase in AMT level makes NP curve (Fig. 11b) prolong to a larger distance ending at catchment-6 and lag = -2. Further development in the MI and resultant NP curve due to the increase and decrease AMT level is as shown in Table-7. In view of the AMT variation analysis there is no trend no dominant mechanism found in the linear behaviour (LP) of the river flow. However, The positive increment in the normally simulated ATM values make a short cyclic affect in the NP curve ending catchment and lag values from +1°C to +6°C. This cyclic affect indicates the influence of the positive temperature rise in nonlinear information propagation. It is to be saying that the temperature variations may introduce some way of nonlinear behaviour in the TDF.





**Fig. 10** Variations in the LIPR curve (based on CC value curves behaviour of the MTDRF along the EDRN from catchment-9 with itself and with all its selected upstream stations) at four different deviations in the normally simulated AMT values: (a) 1°C increase, (b) 4°C increase, (c) 5°C increase, (d) 1°C decrease, (e) 2°C decrease, (f) 5°C decrease and (g) 7°C decrease



**Fig. 11** Variations in the NLPR curve (based on NCMi value curves behaviour of the MTDRF along the EDRN from catchment-9 with itself and with all its selected upstream stations) at four different deviations in the normally simulated AMT values: (a) 1°C increase, (b) 2°C increase, (c) 3°C increase, (d) 1°C decrease, (e) 2°C decrease, and (f) 4°C decrease

**Table 7** Impact of  $\pm^\circ\text{C}$  variations in the annual mean temperature on the LIPR and NLPR curves behaviour that starts from Catchment-9, Lag-0

Temperature Variations ( $^\circ\text{C}$ )	Fall of Propagation of LIPR curves		Fall of Propagation of NLPR curves	
	Catchments No.	Lag No.	Catchments No.	Lag No.
+7	1	-4	6	-1
+6	1	-4	6	-1
+5	1	-4	6	-2
+4	1	-4	7	-2
+3	1	-5	6	-1
+2	1	-5	6	-2
+1	1	-5	7	-2
Normal	1	-4	7	-1
-1	1	-4	7	-1
-2	1	-3	7	-2
-3	1	-3	7	-2

-4	1	-3	6	-1
-5	1	-4	6	-1
-6	1	-4	6	-1
-7	1	-4	6	-1

#### 4 Conclusion

In this paper climatic variability analysis was performed for the simulated model of the Indus River network. The response of variability of the climatic parameter values in the simulated models was recorded. The results obtained from the simulated modelling analysis are very promising. They also strengthen the idea of linear and nonlinear characterisation of influential role of the local climatic parameters. It is may be found that the precipitation influences the TDF propagation in linear way. Moreover, a small impact of positive increase in the precipitation values exhibits nonlinear impact in the propagation of TDF. It follows that for

the TDF propagation the dominant precipitation characteristic is linear. Moreover, it may be explore that the temperature variations make some way of nonlinear behaviour in the TDF propagation.

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